

A combined pool/bilateral dispatch model for electricity markets with security constraints

Um modelo combinado de despacho pool/bilateral para mercados
elétricos com restrições de segurança

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elétricos con restricciones de seguridad

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Abstract

The secure operation of the electric power system is a challenging task for the system operator which is responsible of its coordination, control and monitoring. In most power systems security is typically handled on a multi-state approach. In which case, security criteria are incorporated by means of additional constraints, modifying the initial dispatch calculation. In this paper a generation dispatch model for competitive energy markets considering security constraints is presented. The proposed approach combines the generation dispatch related to pool and bilateral markets with coupled post-contingency optimal power flows into a single optimal dispatch model, avoiding economic

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ineficiências that appear in conventional multi-stage dispatch approaches. The proposed model is linear, and as such, it is based on a DC model of the network. A 6-bus didactic system and the IEEE RTS-24 bus test system are used in order to show the operation and effectiveness of the proposed approach and to compare it with the basic pool/bilateral dispatch with no security constraints. Results show that the inclusion of security constraints lead to a higher dispatch cost. Furthermore, it was found that the enforcement of firmed bilateral contracts might lead to system congestion.

Key words: optimal dispatch, bilateral contracts, energy markets.

Resumo

A operação segura do sistema de potência constitui uma questão difícil para o operador do sistema, o qual é responsável pela coordenação, controle e monitoramento deste. Na maioria dos sistemas de potência a segurança é manejada mediante uma metodologia multi-étapa. Neste caso, os critérios de seguridade são incorporados mediante restrições adicionais as quais mudam o cálculo do despacho inicial. Neste artigo é apresentado um modelo de despacho de geração para mercados elétricos competitivos considerando restrições de segurança. A metodologia proposta combina o despacho de geração de mercados tipo pool e contratos bilaterais com fluxos de potência ótimos post-contingência, acoplados em um modelo de despacho só, o qual evita ineficiências econômicas que aparecem nos despachos convencionais multi-étapa. O modelo proposto é linear, e como tal, é baseado no modelo de rede DC. Um sistema didático de 6 barras e o sistema IEEE RTS-24 são utilizados para ilustrar a operação e efetividade da metodologia proposta e comparar com o despacho pool/bilateral básico, sem restrições de segurança. Os resultados mostram que a inclusão de restrições de segurança leva a um despacho mais caro. Além disso, encontrou-se que a aplicação de contratos bilaterais pode levar a problemas de congestionamento no sistema.

Palavras chaves: despacho ótimo, contratos bilaterais, mercados de energia.

Resumen

La operación segura del sistema de potencia es una tarea difícil para el operador del sistema, el cual es responsable por la coordinación, control y monitoreo de éste. En la mayoría de los sistemas de potencia, la seguridad es manejada mediante una metodología multi-étapa. En este caso, los criterios de seguridad son incorporados mediante restricciones adicionales que modifican el cálculo de despacho inicial. En este artículo se presenta un modelo de despacho de generación para mercados eléctricos competitivos considerando restricciones de seguridad. La metodología propuesta combina el despacho de generación de mercados pool y contratos bilaterales con flujos de potencia óptimos post-contingencia acoplados en un solo modelo de despacho, lo cual evita ineficiencias económicas que aparecen en los despachos convencionales multi-étapa. El

modelo propuesto es lineal, y como tal, se basa en el modelo DC de la red. Un sistema didáctico de seis barras y el sistema IEEE RTS-24 son utilizados para ilustrar la operación y efectividad de la metodología propuesta y para compararlo con el despacho pool/bilateral básico sin restricciones de seguridad. Los resultados muestran que la inclusión de restricciones de seguridad lleva a un despacho más costoso. Por otra parte, se encontró que la ejecución de contratos bilaterales firmes puede llevar a problemas de congestión en el sistema.

Palabras claves: despacho óptimo, contratos bilaterales, mercados de energía.

1 Nomenclature

The following nomenclature is used throughout the paper.

Indices and sets

i: Generator index.

j: Fictitious generator index.

n, m: Node indexes.

lmn: Index of line connecting nodes *m, n*.

k: Contingency index.

L: Set of lines.

N: Set of nodes.

Ng: Set of generators.

Nfg: Set of fictitious generators representing load shedding.

Nd: Set of loads.

Parameters

a: Quadratic coefficient of the bid cost curve ($\$/MW^2h$).

b: Linear coefficient of the bid cost curve ($\$/MWh$).

c: Independent term of the bid cost curve ($\$/h$).

$C_i(Pg_i)$: Bid cost curve of generator i .

$C_j(Pfg_j)$: Bid cost curve of fictitious generator j .

GD : Matrix of bilateral contracts (MW).

Pd : Vector of active power demands (MW).

R^k : Probability of the system to operate under contingency k (%).

Δ_i : Ramp limit of generator i (MW/h).

Pg_i^{Min} : Minimum active power limit of generator i (MW).

Pfg_j^{Min} : Minimum active power limit of fictitious generator j (MW).

Pg_i^{Max} : Maximum active power limit of generator i (MW).

Pfg_j^{Max} : Maximum active power limit of fictitious generator j (MW).

x_{mn} : Reactance of line connecting nodes m, n (Ohms).

F_{lmn}^{Min} : Minimum power flow in line connecting nodes m, n (MW).

F_{lmn}^{Max} : Maximum power flow in line connecting nodes m, n (MW).

Variables

θ_n : Angle of node n (radians).

Pg : Vector of power generation (MW).

F_{lmn} : Power flow in line lmn (MW).

2 Introduction

The dispatch problem arises from the moment in which two or more generators must supply several loads, forcing the system operator to optimally distribute the loads among these generators. Historically, the first optimization efforts were performed over generation control, what is known nowadays as classic economic dispatch [1]. Greater capacity of computer processing along with new techniques for efficient treatment of sparse matrixes have allowed the solution of problems that include network constraints and reliability criteria. This evolution has led to what nowadays is known as Optimal

Power Flow (OPF) [2]. In the last decade the energy sector has undergone fundamental changes. Most of these changes are related to the new trend of unbundling operation of electrical power systems which aims to increase competition and reduce regulation. Under these challenging tasks, the study of economic models and their adaptation to new regulatory frameworks has been of great interest in recent years [3]–[4].

There are several studies that approach the optimal dispatch on an OPF basis. Reference [5] presents a generation scheduling model considering security constraints. Such model is adapted to the Spanish electricity market rules in which the pool-based daily market and the technical constraints are solved in a two-stage basis. That is, after the market clearing procedure has been performed, a second optimization process is carried out redispatching previously matched energy to account for network constraints. Reference [6] presents an AC dispatch using a security-constraint unit commitment model. The proposed solution for the hourly scheduling of generation units is found using Benders decomposition. References [7] and [8] incorporate wind power in the classical dispatch and unit commitment problem. In [9] the dispatch problem is solved using a particle swarm optimization technique, in [10] the dispatch problem is approach through a combination of genetic algorithms, sequential quadratic programming and the maximum entropy principle. Reference [11] presents a comparative study of heuristic techniques applied to the load dispatch problem. In this paper we propose a combined pool-bilateral dispatch model considering contingency constraints. The main purpose of this paper is to show the impact of firm bilateral contracts in a security-constrained dispatch. Integer variables regarding the unit commitment of generating units are not considered. Furthermore, a DC model of the network has been used, therefore, the proposed pool/bilateral dispatch model can be solved using conventional linear programming. A bilateral contract is a privately negotiated instrument that establishes a price and quantity traded between the generation and demand side of the market without intervention of the system operator [12]. Bilateral contracts offer financial stability to generators and lower prices to consumers when compared with the more volatile pool market prices. In the pool model, suppliers and consumers submit their bids in a power auction coordinated by the pool. The pool market is cleared by the system operator, which calculates the market clearing prices through an optimization procedure. In most cases, security constraints are included in

a different market stage, introducing corrections to the previous dispatch [5]. The introduction of corrections in a later stage leads to economic inefficiencies in the dispatch calculation. In this case, we use the term economic inefficiency referring to the attainment of suboptimal solutions. This is supported by the fact that an optimal mathematical solution of a contingency–constrained dispatch is not guaranteed under a multiple–stage process [13]. To avoid such economic inefficiencies, the dispatch with the security constraints must be solved in a single–step procedure. A first attempt to introduce security constraints in a pool/bilateral dispatch model is presented in [14]. The philosophy of the methodology presented in [14] is based on the consideration of feasibility after single contingencies developed by Stott and Alsac in 1974 [15]. The main disadvantage of this methodology is that it is based on an iterative procedure, and thus, as it was already stated, such procedure does not guarantee the achievement of an optimal mathematical solution. To obtain an optimal solution it is necessary to consider all contingencies simultaneously; this is possible using coupled post–contingency power flows in the problem formulation. This approach was first proposed in the literature in [16] in a general context of locational based pricing and reserve markets. Some applications of this approach have been implemented in the context of optimal power flow [17] and energy reserve markets [18].

3 Dispatch in pool and bilateral markets

Under a deregulated market environment, suppliers and consumers are allowed to trade in pool and bilateral markets. In this context, the vectors of active power generation and demand are partitioned to represent pool and bilateral components as shown in (1) and (2).

$$Pg = Pg^p + Pg^b \tag{1}$$

$$Pd = Pd^p + Pd^b, \tag{2}$$

where g and d stand for generation and demand, respectively; and the upper scripts p and b stand for pool and bilateral, respectively. According to the notation developed in [19], GD represents a square matrix of bilateral contracts. Where each element $GD(i, j)$ represents the energy traded between the generator located at bus i , and the load located at bus j . Using this

matrix and a column vector of ones e , the bilateral component of the active power and demand vectors presented in (1) and (2) can be rewritten as in (3) and (4).

$$Pg^b = GD.e \quad (3)$$

$$Pd^b = GD^T.e. \quad (4)$$

In this model bilateral contracts are assumed to be firm, which means that accounting for losses and congestion is responsibility of the pool. The combined pool/bilateral dispatch approach was proposed in a series of papers [20], [21] and [22]. The basic problem involving inelastic demand and firm bilateral contracts is presented as a minimization problem given by (5)–(11).

$$Min \quad \sum_{i \in Ng} C_i(Pg_i) \quad (5)$$

$$Pg_m - Pd_m = \sum_{n \in \Omega N} F_{lmn}; \quad \forall m \in N \quad (6)$$

$$F_{lmn} = (\theta_m - \theta_n) / x_{mn}; \quad \forall lmn \in L \quad (7)$$

$$F_{lmn}^{Min} \leq F_{lmn} \leq F_{lmn}^{Max}; \quad \forall lmn \in L \quad (8)$$

$$Pg_i^{Min} \leq Pg_i \leq Pg_i^{Max}; \quad \forall i \in Ng \quad (9)$$

$$Pg_i \geq Pg_i^b = GD.e; \quad \forall i \in Ng \quad (10)$$

$$\theta_{ref} = 0. \quad (11)$$

The objective function, given by (5), is to minimize the total generation cost, taking into account the active power balance constraints given by (6); the transmission limits given by (7) and (8); the generation limits given by (9); and the set of firm bilateral contracts given by (10). These additional inequality constraints establish minimum generation levels dictated by the bilateral contracts, and distinguish the formulation from the pure pool dispatch.

4 Pool/bilateral dispatch with security constraints

There are two important modeling aspects that are not considered in (5)–(11), namely: the voltage/reactive power representation, and the security

constraints. The first aspect is addressed in [23] and is out of the scope of the present discussion. On the other hand, the security constraints are modeled by means of post-contingency optimal power flows coupled by ramping limits constraints. A ramping limit is understood as how fast a generator can change (increase or diminish) its output in order to minimize load shedding. The proposed model is presented in (12)–(20). Where the upper subscript k stand for the contingency, being $k = 0$ the base case. In this case a contingency consists on the failure of a line or transformer. In the present formulation only single contingencies have been considered, however, the model can be easily expanded to include multiple contingencies. Furthermore, the set of constraints related to bilateral contracts are only considered in the base case and not under contingencies. That is because in the proposed model, the security of the system prevails over the accomplishment of the bilateral contracts. In order to avoid unfeasibility after contingencies we have introduced fictitious generators in load buses. Such generators guarantee the enforcement of power balance constraints and represent load shedding. Consequently, the objective function consists in minimizing the generation and load shedding cost.

$$Min \quad \sum_{k \in K} \sum_{i \in Ng} R^k C_i (Pg_i^k) + \sum_{k \in K} \sum_{i \in Nfg} R^k C_j (Pfg_j^k) \quad (12)$$

$$Pg_m^k - Pd_m^k = \sum_{n \in \Omega N} F_{lmn}^k; \quad \forall m \in N, \forall k \in K \quad (13)$$

$$F_{lmn}^k = (\theta_m^k - \theta_n^k) / x_{mn}; \quad \forall lmn \in L, \forall k \in K \quad (14)$$

$$F_{lmn}^{Min} \leq F_{lmn}^k \leq F_{lmn}^{Max}; \quad \forall lmn \in L, \forall k \in K \quad (15)$$

$$Pg_i^{Min} \leq Pg_i^k \leq Pg_i^{Max}; \quad \forall i \in Ng, \forall k \in K \quad (16)$$

$$Pfg_j^{Min} \leq Pfg_j^k \leq Pfg_j^{Max}; \quad \forall j \in Nfg, \forall k \in K \quad (17)$$

$$Pg_i^0 \geq Pg_i^b = GD.e; \quad \forall i \in Ng \quad (18)$$

$$\left| Pg_i^0 - Pg_i^k \right| \leq \Delta_i; \quad \forall i \in Ng \quad (19)$$

$$\theta_{ref}^k = 0; \quad \forall k \in K. \quad (20)$$

The probability of the system to operate on the base case (without any contingency) is the unit minus the sum of the probabilities of single failure of

all lines and transformers as shown in (21).

$$R^0 = 1 - \sum_{k \in K} R^k . \quad (21)$$

To approach the optimization problem given by (12)–(20), we use the methodology proposed in [16] and [17] which consists in artificially building an equivalent power system composed by islands. These islands correspond to the initial system (base case without contingencies) and to the system after each of the contingencies. The dimensions of such equivalent system are presented in table 1.

Table 1: dimensions of the equivalent system for contingency analysis

Element	Initial system	Equivalent system
Generators	N_g	$(N_g + N_d) * (L + 1)$
Loads	N_d	$(N_g + N_d) * (L + 1)$
Lines	L	$L * L$
Nodes	N	$N * (L + 1)$

5 Test and results

In order to show the validity of the proposed approach several tests were performed with the Wood and Wolleberg 6 bus power system [24] and the IEEE–RTS 24 bus test system [25]. The analysis is based on the performance of the network with and without security constraints, and the increment of firm bilateral contracts. All tests have been performed in Matlab using the linprog function. However, any other LP solver can be used.

5.1 Case 1: 6 bus test system

The Wood and Wolleberg 6 bus power system is shown in figure 1. Tables 2 and 3 summarize the system data. In this case, for the sake of simplicity, we have considered up and down ramps to have the same value. The bid cost curve of the generators is given by (22) and the bilateral contracts are expressed by the GD matrix shown in (23). This matrix represents the energy

traded between generators and loads, for example, $GD(3, 6) = 78$ means that the generator in bus 3 has a firm bilateral contract for 78 MW with the load located in bus 6. Note that the sum of the columns for all bilateral contracts in GD matches the total system demand in nodes 4, 5 and 6.

$$C(Pg) = aPg^2 + bPg + cPg^{Min}. \quad (22)$$

$$GD = \begin{bmatrix} 0 & 0 & 0 & 30 & 40 & 10 \\ 0 & 0 & 0 & 20 & 20 & 12 \\ 0 & 0 & 0 & 20 & 20 & 78 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}. \quad (23)$$

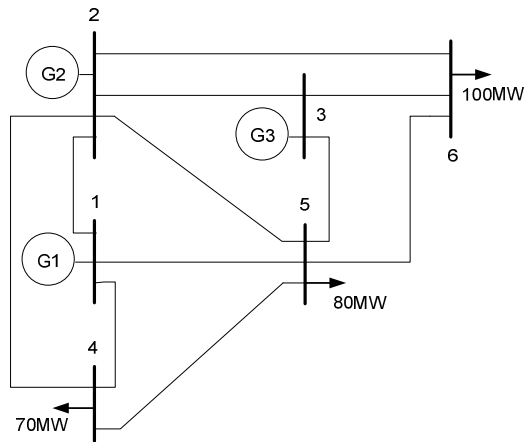


Figure 1: 6 bus power system

Table 2: generators data

Generator	Bus	Pg Min (MW)	Pg Max (MW)	Ramp (MW/h)	a (\$/MW ² h)	b (\$/MWh)	c (\$/h)
G1	1	0	200	30	0.00533	11.669	213
G2	2	0	150	35	0.00889	10.333	200
G3	3	0	180	25	0.00741	10.833	240

Table 3: transmission system data

Line	x	Limit (MW)	R (%)
1-2	0.10	40	0.032
1-4	0.05	60	0.017
1-5	0.08	80	0.025
2-3	0.05	40	0.012
2-4	0.05	60	0.037
2-5	0.10	30	0.011
2-6	0.07	80	0.020
3-5	0.12	70	0.018
3-6	0.02	80	0.035
4-5	0.20	20	0.027
5-6	0.10	40	0.033

The tests were performed using a DC model of the network, and are focused on the comparison between the combined pool/bilateral dispatch with and without security constraints. In order to avoid unfeasibility problems and to represent load shedding, fictitious generators were located in load buses with cost coefficients a and b equal to 200 $\$/MWh$ and 500 $\$/MWh$, respectively. These coefficients model the cost of load shedding.

One of the main purposes of the simulations is to evaluate the impact of firm bilateral contracts in the overall security of the system. This impact is evaluated by performing a series of dispatch solutions where the bilateral contracts are gradually increased. This is accomplished by working with the parameterized matrix $GD(\rho) = \rho \cdot GD$; $0 \leq \rho \leq 1$. Note that when $\rho=1$, the demand is fully supplied by the bilateral contract market, on the other hand, when $\rho=0$, the demand is fully supplied by the pool market. Table 4 shows the bilateral contracts for $\rho=0.7$ and 0.8.

Table 4: bilateral contracts between loads and generators

	$\rho=0.7$			$\rho=0.8$		
	G1	G2	G3	G1	G2	G3
Load bus 4	21	7	14	24	8	16
Load bus 5	28	14	14	32	16	16
Load bus 6	7	8.4	54.6	8	9.6	62.4
Tot Gen	56	29.4	82.6	64	33.6	94.4

5.1.1 Pool/bilateral dispatch without security constraints. Several tests were carried out with different values of the parameter ρ . Table 5 summarizes the results obtained.

Table 5: pool/bilateral dispatch without security constraints

	$\rho=0$	$\rho=0.7$	$\rho=0.8$
Pg1 (MW)	51.08	56.00	72.71
Pg2 (MW)	105.76	103.53	82.88
Pg3 (MW)	93.15	90.46	94.4
Total Cost (\$/h)	2875.7	2876.0	2882.9
Lambda (\$/h)	12.213	12.173	–

In the first run ρ was set to zero letting the demand being fully supplied by the pool market. In this case, the pool market prices, named as lambda (defined as the Lagrange multipliers of the active power balance equations) are the same for all buses (12.213\$/h). That is because there is no congestion and the effect of power losses has been neglected. In the second case, with $\rho=0.7$ the constraint related to the accomplishment of the bilateral contracts for generator $G1$ is active (see total generation in table 3). Consequently, generator $G1$ is set to produce 56 MW. The dispatch is then modified as shown in the second column of table 4. As the output of generator $G1$ was increased, the outputs of generators $G2$ and $G3$ were decreased (to keep the generation/demand balance). The pool market prices are again the same for all buses (no congestion and no losses) however, they are lower than in the first case. That is because the marginal generators ($G2$ and $G3$) reduced their output. In this case, generator $G1$ is said to be “out of merit” and any incremental demand will be supplied either by generator $G2$ or $G3$ at the same marginal price. In the third case studied, the parameter ρ was set to 0.8. In this case, the constraint related to the accomplishment of bilateral contracts for generator $G3$ is active. Consequently, generator $G3$ is set to produce 94.4 MW. The enforcement of the bilateral contracts leads to congestion on line 3–6 causing the pool market prices to be different in all buses. The pool market prices for this case are shown in table 6.

Table 6: Lagrange multipliers with $\rho=0.8$

bus	1	2	3	4	5	6
Lamba (\$/h)	12.44	11.80	-1.85	12.25	13.26	28.83

It can be observed that the marginal price of bus 3 is negative. This means that a decrement in the output of generator $G3$ will lead to an improvement of the objective function. Furthermore, it can be observed, from table 5, that the enforcement of the constraints related to firm bilateral contracts leads to higher operational cost.

5.1.2 Pool/bilateral dispatch with security constraints. The same tests presented in the previous section were carried out considering security constraints. Results are reported in table 7.

Table 7: pool/bilateral dispatch with security constraints

	$\rho=0$	$\rho=0.7$	$\rho=0.8$
Pg1 (MW)	67.85	64.86	72.71
Pg2 (MW)	102.86	102.53	82.88
Pg3 (MW)	79.27	82.60	94.4
Total cost (\$/h)	2878.7	2876.1	28829
Lambda (\$/h)	12.359	12.327	–

To account for the contingency constraints, an equivalent system composed by islands is built. The equivalent system consists on the base case (initial topology without contingencies) and the system after each of the contingencies. The different islands of the equivalent system are coupled with ramping limit constraints. A ramp limit imposes an upper/lower boundary in the change of generation after each contingency with respect to the generation in the base case, see (19). As the objective function considers not only the generation in the base case, but also the generation after each of the contingencies (including the fictitious generators that account for eventually load shedding), the result is a dispatch scheme that minimizes the cost of operation and the expected load shedding. From table 7 it can be observed that when security constraints are considered, the pool market prices as well as the operational cost are slightly higher. In this particular case, accounting for security constraints does not have a great impact in the total operating cost. However, the differences between the dispatch schemes are important. For example, when firm bilateral contracts are not considered, generator $G1$ produces 51.08 MW in the traditional model (table 5) and 67.85 MW in the security constraint model. However, when there is an important participation of bilateral contracts ($\rho=0.8$) both models achieve the same optimal solution.

5.2 Case 2: IEEE RTS-24 bus test system

Figure 2 shows the IEEE-RTS 24 bus test system. The original data of this system can be consulted in [25]. This system comprises 38 lines, 11 generators and 17 loads. Some modifications have been considered in loads, power line limits and generation as shown in tables 8, 9 and 10, respectively. Generators have been divided in three types. For each type, a different bid cost function was considered, ranging from the cheapest (type 1) to the most expensive (type 3). Table 11 shows the bilateral contracts considered.

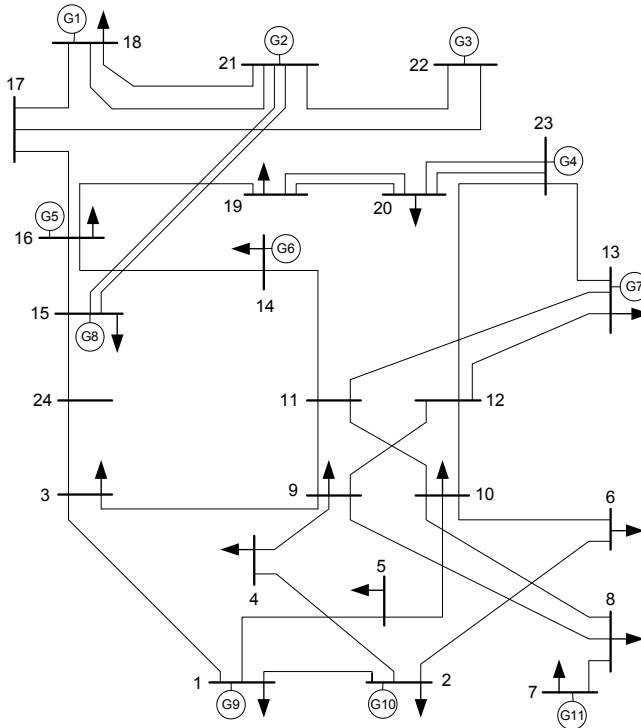


Figure 2: IEEE RTS-24 bus test system

5.2.1 Optimal dispatch without security constraints. The optimal dispatch without bilateral contracts and without security constraints is presented in table 12. It can be observed that the cheapest generators (type 1)

Table 8: limits in power lines

Line	Limit (MW)	Line	Limit (MW)	Line	Limit (MW)	Line	Limit (MW)
1-2	100	7-8	400	12-23	160	17-22	55
1-3	200	8-9	150	15-24	160	18-21	50
1-5	300	8-10	150	13-23	200	18-21	50
2-4	200	9-11	100	14-16	150	19-20	70
2-6	150	9-12	150	15-16	160	19-20	70
3-9	150	10-11	150	15-21	150	20-23	180
3-24	150	10-12	100	15-21	150	20-23	180
4-9	100	11-13	160	16-17	150	21-22	100
5-10	150	11-14	250	16-19	200		
6-10	150	12-13	160	17-18	50		

Table 9: demand in load buses

Bus	Demand (MW)	Bus	Demand (MW)	Bus	Demand (MW)
1	108	7	100	15	317
2	97	8	71	16	225
3	80	9	75	18	333
4	74	10	95	19	281
5	71	13	265	20	240
6	124	14	294		

Table 10: generators data

Generator	Type	Pg Min (MW)	Pg Max (MW)	Ramp (MW/h)	a (\$/MW ² h)	b (\$/MWh)	c (\$/h)
G1, G2, G3, G4	1	50	450	40	0.00563	12.795	215
G4, G6, G7, G8	2	50	300	30	0.00741	15.955	240
G9, G10, G11	3	50	150	10	0.00925	18.564	250

Table 11: bilateral contracts between loads and generators

	G9	G10	G11
Load bus 18	50	50	50
Load bus 19	50	50	50
Load bus 20	40	25	0
Tot Gen	140	125	100

are dispatched at their maxima. On the other hand, the second and third groups of generators are dispatched at 230.05 and 43.26 MW, respectively. In this case, there is no congestion in transmission lines, and generators of types 2 and 3 are dispatched at a level in which the marginal costs of their bidding curves are equal. Such marginal cost is 18.78\$/h, and represents the pool market price. The total operation cost of this dispatch is 165339.30\$/h.

Table 12: dispatch without security constraints

Generator	Type	Dispatch (MW)
G1, G2, G3, G4	1	450.00
G5, G6, G7, G8	2	230.05
G9, G10, G11	3	43.26

5.2.2 Optimal dispatch with security constraints. In this example multiple contingencies were considered as shown in table 13. The lines selected for the contingencies are those which cause the greatest impact in the system in terms of load shedding as reported in [26]. For the three contingencies under study, the same probability of 0.001% has been used. The structure of the equality and inequality constraints matrices of the equivalent system are shown in figures 3 and 4 respectively. Such figures are obtained by a spy-plot in Matlab. In the upper right part of figure 3 four dots equally spaced descending from left to right can be easily spotted. These dots correspond to the constraints of the slack bus for the base case and each of the three contingencies. The remaining of the figure corresponds to the active power balance constraints. The upper left portion of figure 4 corresponds to the power limit constraints in lines and transformers. The middle right portion of figure 4 corresponds to the active power limits constraints of generators, and the lower portion corresponds to the up and down ramp limits.

Table 13: contingencies of multiple lines

Contingency	Line	Line
1	11-13	11-14
2	12-13	12-23
3	11-13	15-24

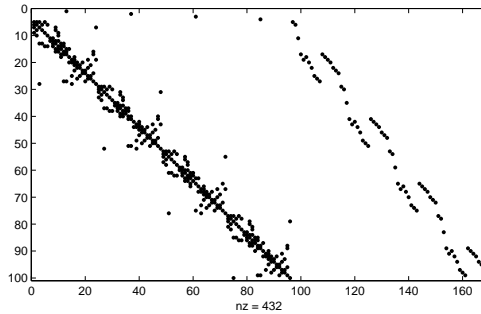


Figure 3: structure of the equality constraints matrix

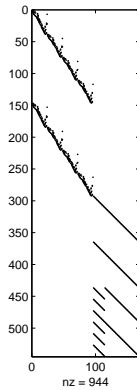


Figure 4: structure of the inequality constraints matrix

The optimal dispatch that minimizes load shedding for these contingencies is shown in table 14. It can be observed that type 1 generators are not dispatched at their maxima, and instead, the output of type 3 generators (the most expensive) has been increased. The differences between the dispatches presented in tables 12 and 14 are due to the security constraints. In order to reduce load shedding after a contingency, more expensive generation has to be used. The cost of this dispatch is 177548.84\$/h representing an increase of 7.38% with respect to the dispatch without contingencies. The pool market prices are 17.12\$/h for all buses. Comparing to the case without contingency constraints, these prices are lower. That is because there is generation available from the cheapest generators (type 1), as opposed to the first case in which these generators were dispatched at their maxima.

Table 14: dispatch with security constraints

Generator	Type	Dispatch (MW)	Generator	Type	Dispatch (MW)
G1	1	431.48	G7	2	245.19
G2	1	429.81	G8	2	240.37
G3	1	409.63	G9	3	50.51
G4	1	410.00	G10	3	51.35
G5	2	235.86	G11	3	108.04
G6	2	237.82			

Table 15 shows the dispatch considering the firm bilateral contracts presented in table 11. The enforcement of these contracts leads the system to congestion in the corridor 18–21 and line 17–22. Consequently, the pool market prices in all nodes are different as shown in table 16. The marginal prices correspond to the dual variables (Lagrange multipliers) of the power balance equations (equality constraints), and as such they indicate the cost of consuming an additional megawatt in a given bus. It can be observed in table 16 that the marginal price in node 22 is negative. That means that an increase of demand (or alternatively, a decrease in generation) will improve the objective function. In this node generator *G11* is located. This generator belongs to the group of the most expensive generators, and regardless of its bilateral contracts it is always dispatch above 100 MW to improve the security of the system. Most of the over cost when considering contingency constraints is due to the high dispatch of this generator (see tables 12 and 14).

Table 15: dispatch with security constraints and bilateral contracts

Generator	Type	Dispatch (MW)	Generator	Type	Dispatch (MW)
G1	1	4.166.749	G7	2	2.889.511
G2	1	4.171.870	G8	2	2.156.736
G3	1	4.190.803	G9	3	1.400.000
G4	1	4.100.000	G10	3	1.250.000
G5	2	681.975	G11	3	1.115.876
G6	2	2.376.480			

Table 16: pool market prices considering security constraints and bilateral contracts

Bus	lambda (\$/h)	Bus	lambda (\$/h)	Bus	lambda (\$/h)
1	169.622	9	170.978	17	225.594
2	169.839	10	172.531	18	169.222
3	162.770	11	174.198	19	177.542
4	170.465	12	173.565	20	176.618
5	171.044	13	174.363	21	104.561
6	171.886	14	176.488	22	-283.827
7	171.754	15	148.997	23	176.115
8	171.754	16	178.619	24	154.260

6 Conclusions

This paper proposes a one-step optimal power flow model that dispatches the pool in combination with firm bilateral contracts considering security constraints. The basic purpose of this paper is to analyze the impact of post-contingency security constraints in a combined pool/bilateral dispatch approach. The tests performed focused on the comparison between the traditional model and the model with security constraints. As expected, the overall dispatch costs are higher when security constraints are accounted for. Furthermore, it was found that the enforcement of firm bilateral contracts (when they are above certain limits) might lead the system to congestion.

The main contribution of the proposed methodology is the inclusion of contingency constraints in a pool/bilateral market scheme using a one-step approach. The proposed methodology adequately handles contingency constraints. However its main drawback consists on the size of the equivalent system; which might render the problem intractable for large power systems, especially when multiple contingencies are considered. This inconvenient can be contoured using specialized procedures for efficient handling of sparse matrices. Future work will include this kind of procedures, as well as a more detailed description of the network and market rules.

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